## Math 1 - Unit 1 Review Function Families

Name

## My child studied for the Unit 1 Test. I am aware that tests are worth $40 \%$ of my child's grade.

## Parent Signature

$\qquad$

## MM1A1 a. Represent functions using function notation. (YELLOW)

## Looking at the table, answer questions 1 and 2.

| Age of Julia | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Height in <br> inches | 30 | 33 | 38 | 40 | 44 | 50 | 55 | 58 | 60 |

1) What is Julia's height at age 5 ? $\qquad$ Express this in function notation. $\qquad$
2) When Julia is 38 inches tall, how old is she? $\qquad$ Express this in function notation. $\qquad$
3) Bananas cost $\$ .75$ per pound at the local grocery store.

Write a function in function notation that models the cost of $x$ pounds of bananas. $\qquad$
Find the cost for 5.3 pounds of bananas. $\qquad$
4) It costs $\$ 10$ to join a movie rental club. After you join, it costs $\mathbf{\$ 3 . 0 0}$ to rent a DVD.

Write a function in function notation that models the cost to join and rent x number of movies. $\qquad$

Find the total cost for joining and renting 5 movies. $\qquad$
5) Decide whether or not the function is written in function notation. Explain how you know. If it is not in function notation, rewrite it in function notation.
a) $g(x)=x^{3}+1$ $\qquad$
b) $f(y)=x-4$
c) $d(t)=t^{2}$
d) $y=5|x|-7$ $\qquad$
6) Given the functions below, find $f(-3), f(0)$, and $f(5)$
a) $f(x)=3 x+7$
b) $f(x)=2 x^{2}$
c) $f(x)=8-x$

MM1A1 b. Graph the basic functions $f(x)=x^{n}$, where $n=1$ to $3, f(x)=x, f(x)=|x|$,and $f(x)=1 / \mathrm{x}$. (HOT PINK)
Write the equation for each parent function. Then draw the graph of the function.
7) Linear:

10) Cubic:

8) Absolute Value: $\qquad$

11) Square Root:

9) Quadratic: $\qquad$

12) Rational: $\qquad$


Read the following statements. Write the name of the function that is being described.
13) This function is undefined at 0 . $\qquad$
14) This function is in the shape of a "V". $\qquad$
15) This function always has a constant rate of change. $\qquad$
16) This function is curvy like a snake or an " $S$ ". $\qquad$
17) This function is in the shape of a parabola. $\qquad$
18) This function has a range from 0 whenever its graph starts on the $y$-axis.

MM1A1 c. Graph transformations of basic functions including vertical shifts, stretches, and shrinks, as well as reflections across the $x$ - and $y$-axes. (GREEN)
19) For the parent function $\mathrm{f}(x)=\sqrt{x}$, how would the function be expressed in function notation if the graph made a vertical shift of 8 ? $\qquad$
20) Create the equation of a cubic function that has a shrink of $1 / 2$ and has been shifted down two units. $\qquad$
21) Write the equation in function notation of a parabola that is reflected and stretched by 2 . $\qquad$
22) Describe the transformations of each of these absolute value functions compared to its parent function.
a) $y=|x|-3$ $\qquad$
b) $y=-|x|+3$ $\qquad$
c) $y=-3|x|$ $\qquad$
d) $y=1 / 3|x|$ $\qquad$

For each transformation of the parent function shown below, identify the parent function and describe the transformation. Then come up with the equation for the new function.

23) Parent Function: $\qquad$
Transformation: $\qquad$
New equation: $\qquad$

24) Parent Function: $\qquad$
Transformation: $\qquad$
New equation: $\qquad$
26) Parent Function: $\qquad$

Transformation: $\qquad$
Transformation: $\qquad$


New equation: $\qquad$
New equation: $\qquad$
27) Parent Function: $\qquad$

Transformation: $\qquad$
28) Parent Function: $\qquad$
Transformation: $\qquad$
New equation: $\qquad$ New equation: $\qquad$

MM1A1 d. Investigate and explain the characteristics of a function: domain, range, zeros, intercepts, intervals of increase and decrease, maximum and minimum values, and end behavior. (BLUE)
29) Describe the following characteristics of the given graph.


Domain: $\qquad$
Range: $\qquad$
X-intercepts/Zeros: $\qquad$
Y-intercepts: $\qquad$
Interval of increase: $\qquad$

Interval of decrease: $\qquad$
Maximum: $\qquad$ and/or Minimum: $\qquad$
End Behavior: $\qquad$
30) Describe the following characteristics of the given graph.


Domain: $\qquad$
Range: $\qquad$
X-intercepts/Zeros: $\qquad$
Y-intercepts: $\qquad$
Interval of increase: $\qquad$
Interval of decrease: $\qquad$
Maximum: $\qquad$ and/or Minimum: $\qquad$
End Behavior: $\qquad$

MM1A1 e. Relate to a given context the characteristics of a function, and use graphs and tables to investigate its behavior. (RED)

Tell whether or not the relation is a function. Explain. Then circle the domain and box the range.

## 31)

| Input | Output |
| :--- | :--- |
| 1 | 3 |
| 2 | 3 |
| 7 | 2 |
| 8 | 2 |

32) 

| Input | Output |
| :--- | :--- |
| 12 | 13 |
| 13 | 14 |
| 13 | 15 |
| 15 | 16 |

33) 


34) Create a table that matches the graph.

| x | -2 | 1 | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| y |  |  |  |  |  |


$y=f(x)$
35) Draw a graph to represent the situation: A car driving 20 mph speeds up to 30 mphs in 5 seconds. It stays that speed for the next 5 seconds. Then it slows to a stop in the next 5 seconds.
36) Does it make sense to connect the dots above? Why or why not? Be sure to include an explanation of discrete or continuous data in your answer.
37) MULTIPLE CHOICE PRACTICE: Which of the following describes the graphs on the right?
A) Tom rode his bike east from his home up a steep hill. After a while the slope eased off. At the top he raced down the other side.
B) Tom took his dog for a walk. He set off slowly and then increased his pace. At the park, Tom turned around and walked slowly back home.
C) Tom went for a jog. At the end of his road, he bumped into a friend and his pace slowed. When Tom left his friend, he walked quickly back home.


Use the graph on the right to answer questions 38-40.
38) Which part of the data is the independent variable? Explain.
39) Which part of the data is the dependent variable? Explain.

Girls' registrations (thousands)
40) As the years increase, do the number of girl soccer players increase or decrease?

Explain. $\qquad$

Girls' Soccer Participation


MM1A1 f. Recognize sequences as functions with domains that are whole numbers. (PURPLE)
41) Refer to the following pattern of dot-figures:


Write the rule for the $n$th term of this sequence $\qquad$

If this pattern of dot-figures is continued, how many dots will be in the 100th figure? $\qquad$
42) Write the first 6 terms of the sequence $a_{n}=3 n-5$. $\qquad$ , $\qquad$ , $\qquad$
$\qquad$
$\qquad$ ,
Show your work here:

Is the sequence above arithmetic or geometric? Explain. $\qquad$

List the domain: $\qquad$ List the range: $\qquad$
43) What is an explicit formula for the sequence $-6,-4,-2,0, \ldots$ ?
$\mathrm{a}_{\mathrm{n}}=$

$$
a_{15}=
$$

44) Consider the sequence $3,9,19,33,51, \ldots$

Is this a finite or infinite sequence? $\qquad$
What is $a_{1}$ ? $\qquad$ What is $a_{3}$ ? $\qquad$

MULTIPLE CHOICE PRACTICE: Which expression can be used to determine the $n$th term in the sequence from above?
A) $6 \mathrm{n}-3$
B) $2 n^{2}+1$
C) $4 n-1$
D) $n^{2}+2$

MM1A1 g. Explore rates of change, comparing constant rates of change(slope)versus variable rates of change. Compare rates of change of linear, quadratic, square root, and other function families. (ORANGE)
45) Write the formula for rate of change:
46) Find the slope of the line with points $(2,-4)$ and $(-3,7)$.

This table shows the total number of paper airplanes Gina made after school over time. Use it to answer \#47 and \#48.
Gina's Paper Airplanes

| Time (in minutes) | 0 | 5 | 10 | 15 | 20 | 25 | 30 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Total Number of <br> Paper Airplanes | 0 | 5 | 10 | 15 | 23 | 31 | 39 |

47) What is Gina's average rate of making paper airplanes during the first 15 minutes she made them? $\qquad$
48) What is Gina's average rate of making paper airplanes during the last 15 minutes she made them? $\qquad$

The table below gives the number of lawn mowers, $l$, sold in a hardware store between 1985 and 1990.

| Year, $t$ | 1985 | 1986 | 1987 | 1988 | 1989 | 1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Lawn mowers, $l$ | 40 | 56 | 72 | 88 | 104 | 120 |

49) Determine which model best fits the data. $\qquad$
50) Find the rate of change from 1987 to 1989. $\qquad$
51) What is the missing value in the table on the right?

Describe its rate of change.
52) This graph shows how far Elena hiked over the course of four hours.

$\qquad$
$\qquad$

Which statement is NOT true about the rates of change shown in the graph?

| $\boldsymbol{p}$ | $\boldsymbol{w}$ |
| ---: | :---: |
| -3 | 14 |
| -2 | 11 |
| -1 | $?$ |
| 0 | 5 |
| 1 | 2 |
| 2 | -1 |

A. The rate of change was 3 miles per hour between 0 and 2 .
B. The rate of change was 0 miles per hous between hours 2 and 3 .
C. The rate of change was 4 miles per hour berween hours 3 and 4 .
D. The rate of change was a constant 2.5 miles per hour berween hours 0 and 4 .

MM1G2 a. Use conjecture, inductive reasoning, deductive reasoning, counterexamples, and indirect proof as appropriate. (LIME GREEN)
53) MULTIPLE CHOICE PRACTICE: Use the graph to the right to make a conjecture that could be true. Choose the best answer below.

Girls' Soccer Participation


For problems 54 and 55, tell whether the statement is true or false. If false, give a counterexample.
54) If $x=-6$, then $x^{2}=36$. $\qquad$
55) If $x^{2}=16$, then $x=4$.
56) MULTIPLE CHOICE PRACTICE: In math class, you notice that every number can be written as a prime factorization. Which factorization of 24 supports this conjecture?
A) $8 \times 3$
B) $12 \times 2$
C) $2 \times 2 \times 2 \times 3$
D) $4 \times 3 \times 2$

Decide whether inductive or deductive reasoning is used. Then explain.
57) Your mom diets for 3 weeks and loses 3 pounds. She concludes that she can lose 20 pounds if she diets for 20 weeks.
58) You use the rise of 8.1 and the run of 2.7 between two points on a line in the coordinate plane to conclude the slope of the line is 3 .
59) On Kelly's math test, the first 3 multiple choice answers were "C." She concludes that the rest of the answers are also "C." $\qquad$

MM1G2 b. Understand and use the relationships among a statement and its converse, inverse, and contrapositive. (PINK)
Underline the hypothesis and circle the conclusion. Then tell whether it's true or false. If false, give a counterexample.
60) If you are a football player, then you are an athlete. $\qquad$
61) If a function has a constant rate of change, then it is linear. $\qquad$

Now, write the converse, inverse, and contrapositive for the statement in \#60. Then decide whether the new statement is true or false.
62) Converse: $\qquad$

True or False? $\qquad$
63) Inverse: $\qquad$

True or False? $\qquad$
64) Contrapositive: $\qquad$

True or False? $\qquad$

